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QUANTUM 1/f NOISE IN SOLID STATE DEVICES  
IN PARTICULAR  $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$  N<sup>+</sup>-P DIODES

FINAL REPORT

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Papers published under the contract July 1, 1985 to date

A. Early papers on which the present contract is based.

1. A. van der Ziel, C. J. Hsieh, P. H. Handel, C. M. van Vliet, and G. Bosman, "Partition 1/f noise in vacuum pentodes," Physica, vol. 124B, p. 299, 1984.
2. A. van der Ziel and P. H. Handel, "Quantum partition 1/f noise in pentodes," Physica, vol. 125B, p. 286, 1984.  
These were the first two papers that indicated the presence of quantum partition 1/f noise in pentodes.
3. A. van der Ziel, P. H. Handel, X. C. Zhu, and K. H. Duh, "A theory of the Hooke parameters of solid-state devices," IEEE Trans. Electron Devices, vol. ED-32, p. 667, 1985.
4. K. H. Duh and A. van der Ziel, "Hooke parameters in various FET structures," IEEE Trans. Electron Devices, vol. ED-32, p. 662, 1985.
5. X. C. Zhu and A. van der Ziel, "The Hooke parameter of  $n^+$ -p-n and  $p^+$ -n-p silicon bipolar transistors," IEEE Trans. Electron Devices, vol. ED-32, p. 658, 1985.  
These were the first papers indicating the possible presence of quantum 1/f noise in FETs and BJTs.

B. Early papers under the contract

6. A. van der Ziel and P. H. Handel, Discussion of a generalized quantum 1/f noise process with applications, Physica, 132B, 367, 1985.  
Quantum 1/f noise process described by lumped model.
7. A. van der Ziel, Theory of and experiments on quantum 1/f noise, in Noise in Physical Systems and 1/f Noise, Eds. A. D'Amico and P. Mazzetti, Elsevier Science Publishers BV, 11, 1986.  
Review paper presented at the Rome Noise Conference, Sept. 1983.
8. X. L. Wu and A. van der Ziel, Experiments on high frequency and 1/f noise in long  $n^+$ -p  $Hg_{1-x}Cd_xTe$  diodes, in Noise in Physical Systems and 1/f Noise, Eds. A. D'Amico and P. Mazzetti, Elsevier Science Publishers BV, 491, 1986.  
Used wrong estimated carrier lifetimes, otherwise correct. First application of the transmission line method.
9. A. van der Ziel and P. H. Handel, "1/f noise in  $n^+$ -p diodes," IEEE Trans. Electron Devices, vol. ED-32, p. 1805, 1985.
10. A. van der Ziel and P. H. Handel, "1/f noise in  $n^+$ -p junctions calculated with quantum 1/f theory," in Noise in Physical Systems and 1/f Noise, Eds. A. D'Amico and P. Mazzetti, Elsevier Science Publishers BV, p. 481, 1986.  
(10) is a better readable version of (9). Discusses recombination-generation and injection-extraction 1/f noise.



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11. X. C. Zhu, X. L. Wu, A. van der Ziel and E. G. Kelso, "The Hooge parameters for n-type and p-type  $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$ ," IEEE Trans. Electron Devices, vol. ED-32, p. 1353, 1985.  
Tables of the Hooge parameter of  $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$   $n^+-p$  diodes versus composition  $x$  and temperature  $T$ .

C. Papers mentioned in the progress reports

12. P. H. Handel and A. van der Ziel, "Relativistic correction of the Hooge parameter for Umklapp  $1/f$  noise," Physica, vol. 141B, p. 145, 1986.  
Relativistic effects become important if  $m < 0.02 m_0$ .
13. A. van der Ziel, P. H. Handel, X. L. Wu and J. B. Anderson, "Review of the status of quantum  $1/f$  noise in  $n^+-p$   $\text{HgCdTe}$  photodiode detectors and other devices," J. Vac. Sci. Technol., vol. A4, no. 4, p. 2205, 1986 (San Diego MCT workshop 1985).  
Extensive review of the status of quantum  $1/f$  noise. Still uses wrong estimated values of  $\tau$  in  $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$ .
14. A. van der Ziel, "Interpretation of Schwantes's experimental data on secondary emission  $1/f$  noise," Physica, vol. 144B, p. 205, 1987.  
Interprets Schwantes' secondary emission  $1/f$  noise as quantum  $1/f$  noise.
15. X. L. Wu, J. B. Anderson and A. van der Ziel, "Diffusion and recombination  $1/f$  noise in long  $n^+-p$   $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$  Diodes," IEEE Trans. Electron. Devices, vol. ED-34, p. 602, 1987.  
Uses the measured values for  $\tau$ . Finds from this value  $\alpha_H = (3-5)10^{-3}$  (coherent state) or  $\alpha_H = 5 \times 10^{-5}$  (Umklapp).
16. A. van der Ziel, C. J. Hsieh, P. H. Handel, C. M. Van Vliet and G. Bosman, "Partition  $1/f$  noise in pentodes and its quantum interpretation," Physica, vol. 145B, p. 195, 1987.  
Expands and slightly corrects earlier work. Most data agree with the quantum  $1/f$  noise theory, but in one noisy device the quantum  $1/f$  noise seems to be masked by noise of non-quantum origin.
17. P. Fang and A. van der Ziel, "Coherent state quantum  $1/f$  noise in long Si p-i-n diodes at elevated temperatures," in Noise Physical Systems, Ed. C. M. Van Vliet, Montreal, May 1987, World Scientific, Singapore, 410, 1987.  
Shows that the devices have coherent state  $1/f$  noise.
18. A. van der Ziel, "Experimental results, possibly involving quantum  $1/f$  noise in devices," in Noise in Physical Systems, Ed. C. M. Van Vliet, Montreal, May 1987, World Scientific, Singapore, 397, 1987.  
Gives a survey of quantum  $1/f$  noise experiments.
19. A. van der Ziel, "Semiclassical derivation of quantum  $1/f$  noise in collision-free devices," in Noise in Physical Systems, Ed. C. M. Van Vliet, Montreal, May 1987, World Scientific, Singapore, 427, 1987.  
First semiclassical interpretation of quantum  $1/f$  noise in terms of Bremsstrahlung fluctuations.

20. Q. Peng, A. Birbas and A. van der Ziel, "A note for experimental results for the Hooke parameters in P-MOSFETs," in Noise in Physical Systems, Ed. C. M. Van Vliet, Montreal, May 1987, World Scientific, Singapore, 400 (1987).  
First semiconductor noise source in which  $\alpha_H$  has an  $L^2$  dependence. Later attributed to acceleration  $1/f$  noise.
21. P. Fang and A. van der Ziel, "Study of secondary emission  $1/f$  noise," Physica, 147B, 311 (1987).  
Verifies the quantum expression for secondary emission  $1/f$  noise term by term.
22. A. van der Ziel, "Unified presentation of  $1/f$  noise in electronic devices; Fundamental  $1/f$  noise sources," Proc. IEEE, 76, 233 (1988).  
First unified presentation of  $1/f$  noise in terms of the Hooke parameter and of fundamental  $1/f$  noise sources. As a side result many quantum  $1/f$  noise formulas are verified experimentally.
23. P. Fang, L. He, Q. Peng, H. Kang, and A. van der Ziel, "1/f noise study in vacuum photodiodes, submitted to J. Applied Physics, 65, 1766 (1989).  
Verifies the quantum expressions for photodiode  $1/f$  noise term by term. Shows that the (classical) noise due to work function fluctuations has a  $1/f^{3/2}$  spectrum (two-dimensional diffusion over the cathode surface).
24. A. van der Ziel, "The experimental verification of Handel's expression for the Hooke parameter," Solid State Electronics, 31, 1205 (1988).  
Based on paper #18, puts chief emphasis on the experimental verification of Handel's expressions.
25. A. van der Ziel, "Semiclassical derivation of Handel's expression for the Hooke parameter," J. Applied Physics, 63, 2456 (1988).  
Extension of the derivation of paper (19) to collision dominated devices.
26. A. van der Ziel, "Generalized semiclassical quantum  $1/f$  noise theory; acceleration  $1/f$  noise in semiconductors," J. Applied Physics, 63, 903 (1988).  
Extends the theory to the acceleration  $1/f$  noise process and shows that in the latter the Hooke parameter varies as the square of the device length  $L$  for intermediate values of  $L$ .
27. Q. Peng, A. N. Birbas, A. van der Ziel, A. D. van Rheeën and K. Amneriadis, "Channel-length dependence of the  $1/f$  noise in silicon metal-oxide-semiconductor field-effect transistors, verification of the acceleration  $1/f$  noise process," J. Applied Physics 63, July 1988, 907, (1988)  
Shows that the Hooke parameter varies as the square of the device length  $L$  for intermediate values of  $L$ , as expected from A. van der Ziel's acceleration  $1/f$  noise process. For larger values of  $L$  saturation effects are expected.
28. P. Fang, L. He, A. D. van Rheeën, A. van der Ziel and Q. Peng, "Noise and lifetime measurements in Si  $p^+i-n$  diodes," Solid State Electronics, (1989), in press.

29. A. van der Ziel, P. Fang, L. He, X. L. Wu and A. D. van Rheelen, "1/f noise characterization of  $n^+p$  and  $n-i-p$   $Hg_{1-x}Cd_xTe$  detectors, J. Vac. Sci Technology, A-7, 550 (1989).
30. A. van der Ziel, Formulation of surface 1/f noise processes in bipolar junction transistors and in p-n diodes in Hooge type form, Solid State Electron, 32, 91 (1989).

D. Papers written during the last eight months of the contract

SECONDARY EMISSION 1/f NOISE REVISITED\*

by A. van der Ziel, P. Fang and A. D. van Rheeën

Abstract

Fang and van der Ziel's analysis of secondary emission 1/f noise in secondary emission pentodes is extended to 16 individual data points. It is found that by proper choice of the secondary electron path length  $d_{da}$ , good agreement between the experimental values of the Hooe parameter  $\alpha_H$  and the theoretical values predicted by Handel's quantum 1/f noise theory is obtained for 14 data points. Handel's equations for the Hooe parameter of the tubes thus seem to have heuristic validity. The values of the secondary electron path length  $d_{da}$  differ somewhat from tube to tube and may also depend slightly on bias; these effects are attributed to the electron-optical system formed by screen grid, dynode and anode.

\* Accepted for publication in Journal of Applied Physics.

EXTENSIONS OF HANDEL'S 1/f NOISE EQUATIONS AND THEIR SEMICLASSICAL THEORY\*\*

by A. van der Ziel, A. D van Rheeën, and A. N. Birbas

Abstract

By replacing the change in velocity  $\Delta \vec{v}$  by the low frequency Fourier transform  $F(\omega)$  of the electron acceleration  $\vec{a}(t)$ , Handel's equations for the Hooe parameter  $\alpha_H$  are put in equivalent forms that are not only applicable to collision 1/f noise in semiconductors but also to acceleration 1/f noise in long devices. When the power spectrum  $S_p(f)$  of the emitted Bremsstrahlung is evaluated, it contains already the two terms  $(q/e)^2$  and  $|F(\omega)|^2/c^2$  found in Handel's extended expressions for the Hooe parameter  $\alpha_H$ . Going over to elementary events and defining the spectrum of the quantum emission rate  $S_q''(f)$  per elementary event by the equation  $S_q''(f) = S_p(f)/[hf\tau_a]$ , where  $\tau_a$  is the duration of the Bremsstrahlung pulse, the expression also contains the factor  $4\alpha_0/(3\pi)$  found in Handel's expression for  $\alpha_H$ . It thus seems that the Hooe parameter depends only on the Bremsstrahlung emission process but not on the details of the electron-photon interaction. This may explain why Handel's expressions for  $\alpha_H$  so often agree with experiment. Introducing the current spectrum  $S_I''(f) = S_I(f)/\lambda$  per elementary event where  $\lambda = N/\tau_a$  and  $N$  the number of carriers, and bearing in mind that  $S_I''(f)$  and  $S_q''(f)$  come from the same quantum process and are therefore proportional, it is highly likely that the proportionality factor corresponds to the shot noise of an elementary event. This leads immediately to the Hooe equation and to the Hooe parameter  $\alpha_H$ .

\*\*Accepted for publication in Physical Review B.



# EXTENSION OF THE HOOGE EQUATION AND OF THE HOOGE PARAMETER CONCEPT\*

by A. van der Ziel and A. D. van Rheelen

## Abstract

The Hooge equation is extended to the case where the noise spectrum is of the form  $1/f^\gamma$  with  $\gamma$  slightly different from unity. This leads to a generalization of the Hooge parameter that corrects an earlier ambiguity.

\* Accepted for publication in Solid-State Electronics.

# GENERATION-RECOMBINATION-TYPE $1/f$ NOISE IN n-i-p DIODES\*\*

by A. van der Ziel, L. He, A. D. van Rheelen, and P. Fang

## Abstract

It is shown for p-i-n diodes, in which the current flow is by hole-electron pair generation and (or) recombination, that the  $1/f^\gamma$  noise is due to generation-recombination processes involving traps and (or) recombination centers and that the spectrum may be written as  $S_I(f) = \alpha_H e |I| / [f^\gamma \tau]$ , where  $\alpha_H$  is the Hooge parameter,  $e$  the electron charge,  $|I|$  the absolute current,  $\tau$  the time constant associated with the pair generation and pair recombination process,  $f$  the frequency and  $\gamma$  is the exponent of the spectrum. This is studied experimentally and the Hooge parameters of various devices are determined.

\*\*Accepted for publication in Solid-State Electronics.

1/f NOISE IN DOUBLE HETEROJUNCTION  
AlGaAs-GaAs LASER DIODES ON GaAs AND ON Si SUBSTRATES \*

by R. Z. Fang, A. C. Young, A. van der Ziel,  
A. D. van Rheeën, and J. P. van der Ziel

Abstract

1/f noise measurements at forward bias are reported on double heterojunction AlGaAs-GaAs laser diodes fabricated on GaAs and on Si substrates. The noise spectrum is of the form  $1/f^\beta$  with  $\beta$  close to unity.  $S_I(f)/I$  is roughly independent of current for  $I < 1\text{ mA}$  and decreases with increasing current for  $I > 1\text{ mA}$ . This means that the Hooge equation is valid for  $I < 1\text{ mA}$  with constant  $\alpha_H/\tau$ , whereas  $\alpha_H/\tau$  decreases with increasing current for  $I > 1\text{ mA}$ . Here  $\alpha_H$  is the Hooge parameter and  $\tau$  the carrier lifetime.

The values of  $\alpha_H/\tau$  for devices on a Si-substrate (#1 and #3) are 20-50 times larger than for devices on a GaAs substrate (#5,6, and 7); this is attributed to the fact that the diodes on a Si-substrate have a much larger dislocation density than the diodes on a GaAs substrate. The current dependence of  $\alpha_H/\tau$  is a high injection effect. For  $I \ll 1\text{ mA}$  the carrier density in the active region is equal to the equilibrium density  $N_0$ , and  $\alpha_H = \alpha_{H0}$  and  $\tau = \tau_0 = 2 \times 10^{-9}\text{ s}$  are constants; for  $I \gg 1\text{ mA}$  there is high injection so that  $N \gg N_0$ .  $\alpha_H$  and  $\tau$  now decrease with increasing  $I$ , and the data require that  $\alpha_H$  decreases faster than  $\tau$ . The diodes with a silicon substrate have  $\alpha_{H0} \approx (2.5-5.0) \times 10^{-3}$  for  $I < 1\text{ mA}$ ; this value for  $\alpha_H$  is probably accidental and does not indicate Hooge type 1/f noise.

\* To be submitted to Journal of Applied Physics.